

IN THE CLAIMS:

Please amend Claims 1, 5, 7, 8 and 11.

Please add Claims 14-16.

1. (Currently Amended) A An image processing method for recovering ~~recovery of recovering~~ 3D a
scene structure and camera motion from successive image data obtained from a multi-image
sequence, wherein a reference image of the sequence is taken by a camera at a reference
perspective and one or more successive images of the sequence are taken at one or more
successive different perspectives by translating and/or rotating the camera, the method
comprising the steps of:

- (a) determining comparing the image data of a reference shifts for each successive
image to the image data of the successive image, the successive image being taken by
translating or rotating the camera with respect to the reference image and the image data being
one or more characteristics selected from a group consisting of points, lines and intensities
with respect to the reference image; the shifts being derived from the camera translation
and/or rotation from the reference perspective to the successive different perspectives;
- (b) constructing a determining the image shift data shift for the successive matrix that
incorporates the image with respect to the reference data shifts for each image;
- (c) calculating two rank 3 factor matrices from the shift data matrix using SVD, one
rank 3 factor matrix constructing shift data representation that incorporate the image data
shifts for each image corresponding to the 3D structure and the other rank 3 factor matrix
corresponding to the camera motion; and

(d) recovering determining the direction of the camera motion and the 3D structure from the shift data representation, 3D structure matrix by solving a linear equation; and

(e) recovering the camera motion from the camera motion matrix using the recovered 3D structure.

2. (Original) The method of claim 1, wherein the image data is one or more selected from the group consisting of points, lines and intensities.

3. (Currently Amended) The method of claim 1, wherein the step of determining the image data shifts includes initially recovering and compensating for camera rotation.

4. (Original) The method of claim 1, wherein step (b) comprises:

computing H and \bar{D}_{CH} , where H is a $(N_{tot} - 3) \times N_{tot}$ matrix and $\bar{D}_{CH} \equiv C^{-1/2} \bar{D} H^T$ and $N_{tot} \equiv 2N_p + 2N_L + N_X$, where N_p , N_L , and N_X equal the number of points, lines and intensities, respectively, and C is a $(N_I - 1) \times (N_I - 1)$ matrix with $C_{ii'} \equiv \delta_{ii'} + 1$ where $C_{ii'}$ is a constant table of values for all images and $\delta_{ii'}$ is an operator equal to 1 if $i = i'$ and 0 if $i \neq i'$, and $\bar{D} \equiv [S \omega_L \Lambda \omega_I \Delta]$, H^T is the transpose of the H matrix, where H is a matrix defined such that H^T is an identity matrix and annihilates $\bar{\Psi}_x, \bar{\Psi}_y, \bar{\Psi}_z$ where $\bar{\Psi}_x^T \equiv [\Psi_x^T \omega_L \Psi_{Lx}^T \omega_I \Psi_x^T]$ and similarly for the y and z components where, ω_I and ω_L are constant weights that the user sets,

and where $\Psi_{Lx} \equiv \begin{bmatrix} \{P_U \cdot (\hat{x} \times A)\} \\ \{P_L \cdot (\hat{x} \times A)\} \end{bmatrix}$, $\Psi_{Ly} \equiv \begin{bmatrix} \{P_U \cdot (\hat{y} \times A)\} \\ \{P_L \cdot (\hat{y} \times A)\} \end{bmatrix}$, $\Psi_{Lz} \equiv \begin{bmatrix} \{P_U \cdot (\hat{z} \times A)\} \\ \{P_L \cdot (\hat{z} \times A)\} \end{bmatrix}$ where A_I is the

unit normal to the plane containing the line and the camera center at the reference image and where $\hat{x}, \hat{y}, \hat{z}$ are unit vectors in the x, y and z directions, and where

$$\Psi_x \equiv \begin{bmatrix} \{r_x^{(1)}(q)\} \\ \{r_y^{(1)}(q)\} \end{bmatrix}, \quad \Psi_y \equiv \begin{bmatrix} \{r_x^{(2)}(q)\} \\ \{r_y^{(2)}(q)\} \end{bmatrix}, \quad \Psi_z \equiv \begin{bmatrix} \{r_x^{(3)}(q)\} \\ \{r_y^{(3)}(q)\} \end{bmatrix} \text{ where } q=(x,y) \text{ is the image position of the}$$

tracked point in the reference image and

the three point rotational flows $r^{(1)}(x,y), r^{(2)}(x,y), r^{(3)}(x,y)$ are defined by

$$[r^{(1)}, r^{(1)}, r^{(1)}] \equiv \left[\begin{pmatrix} -xy \\ -(1+y^2) \end{pmatrix}, \begin{pmatrix} 1+x^2 \\ xy \end{pmatrix}, \begin{pmatrix} -y \\ x \end{pmatrix} \right]$$


and where

$\Psi_{lx} \equiv -\{\nabla I \cdot r^{(1)}(p)\}, \Psi_{ly} \equiv -\{\nabla I \cdot r^{(2)}(p)\}, \Psi_{lz} \equiv -\{\nabla I \cdot r^{(3)}(p)\}$, and where p gives the image coordinates of the pixel positions, and

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where Λ is an $N_i \times 2N_L$ matrix where each row corresponds to a different image i and equals

$$\left[\{P_U \cdot \delta A^i\}^T \{P_L \cdot \delta A^i\}^T \right] \text{ where } P_U \text{ and } P_L \text{ are unit 3-vectors projecting onto two directions}$$

$A_i \times (\hat{z} \times A_i)$ and $\hat{z} \times A_i$ which we refer to respectively as the upper and lower directions,

where δA^i is the line flow $\delta A_i^i \equiv A_i^i - A_i^0$, and \hat{z} is the unit vector in the z direction and

where S is a $N_i \times 2N_p$ matrix where each row corresponds to a different image i and equals

$$\left[\{s_x^i\}^T \{s_y^i\}^T \right], \text{ where } s_m^i \equiv q_m^i - q_m^0 \text{ and denotes the image displacement for the } m\text{-th tracked}$$

point and where Δ is a $N_i \times N_X$ matrix, where each row corresponds to an image i and equals

$$\{\Delta I^i\}^T \text{ where } \Delta I \text{ is the change in image intensity with respect to the reference image and}$$

where I^i denotes the i -th intensity image and where $I_n^i = I^i(p_n)$ denotes the image intensity

at the n -th pixel position in I and where the notation $\{V\}$ is used to denote a vector with elements given by the V^a .

5. (Currently Amended) The method of claim 1, wherein step (c) comprises:

computing a best rank-3 factorization of $\bar{D}_{CH} \approx M^{(3)}S^{(3)T}$ where $M^{(3)}, S^{(3)}$ are rank 3 matrices corresponding respectively to motion and structure, using SVD.

6. (Original) The method of claim 1, wherein step (d) comprises:

eliminating structure unknowns Q_z , B_z and Z^{-1} from the $\bar{\Phi}_a$ to get $3N_{tot}$ linear constraints on the U and Ω using the linear equation, $[\bar{\Phi}_x \bar{\Phi}_y \bar{\Phi}_z] = H^T S^{(3)}U + [\bar{\Psi}_x \bar{\Psi}_y \bar{\Psi}_z]\Omega$, where U and Ω are unknown 3x3 matrices, and $\bar{\Phi}$ and $\bar{\Psi}$ represent total translational and rotational flow vectors respectively, and solving these constraints with $O(N_{tot})$ computations using the

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SVD, where the total translational flow vectors are defined by $\bar{\Phi}_x \equiv \begin{bmatrix} \Phi_x \\ \omega_L \Phi_{Lx} \\ \omega_I \Phi_{Ix} \end{bmatrix}$ and similarly

for the y and z components, and

$\Phi_{Lx} \equiv \begin{bmatrix} \{A_x B_U\} \\ \{A_x B_L\} \end{bmatrix}, \Phi_{Ly} \equiv \begin{bmatrix} \{A_y B_U\} \\ \{A_y B_L\} \end{bmatrix}, \Phi_{Lz} \equiv \begin{bmatrix} \{A_z B_U\} \\ \{A_z B_L\} \end{bmatrix}$ where A is the normal to a first plane that passes through the center of projection and the imaged line in the reference image, and the normal to a second plane, B is defined by requiring $B \cdot A = 0$ and $B \cdot Q = -1$ for any point Q the 3D line L, and where $B_U \equiv B \cdot P_u$ and $B_L \equiv B \cdot P_L$ are the upper and lower components of B, and where

$$\Phi_x \equiv -\begin{bmatrix} \{Q_z^{-1}\} \\ \{0\} \end{bmatrix}, \Phi_y \equiv -\begin{bmatrix} \{0\} \\ \{Q_z^{-1}\} \end{bmatrix}, \Phi_z \equiv -\begin{bmatrix} \{q_x Q_z^{-1}\} \\ \{q_y Q_z^{-1}\} \end{bmatrix}$$

and where

$$\Phi_{lx} \equiv -\{Z^{-1}I_x\}, \Phi_{ly} \equiv -\{Z^{-1}I_y\}, \Phi_{lz} \equiv \{Z^{-1}(\nabla I \cdot p)\}, \text{ and}$$

where Q is the 3d coordinate for a 3D tracked point corresponding to an image pixel in the reference image, and Z_n is the depth from the camera to the 3D point imaged at the n-th pixel along the cameras optical axis; and

recovering the structure unknowns Q_z , B_z and Z^{-1} from

$$[\bar{\Phi}_x \bar{\Phi}_y \bar{\Phi}_z] = H^T S^{(3)} U + [\bar{\Psi}_x \bar{\Psi}_y \bar{\Psi}_z] \Omega, \text{ given } U \text{ and } \Omega.$$

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7. (Currently Amended) The method of claim 1, wherein step (d) further (e) comprises:

using $S^{(3)}U \approx [\bar{\Phi}_x \bar{\Phi}_y \bar{\Phi}_z]$ and

$$\bar{D}_{CH} \approx C^{-\frac{1}{2}} \{T_x\} \bar{\Phi}^T H^T + C^{-\frac{1}{2}} \{T_y\} \bar{\Phi}_y^T H^T + C^{-\frac{1}{2}} \{T_z\} \bar{\Phi}_z^T H^T \text{ to recover the translations, and}$$

recovering the rotations $\omega_x^i, \omega_y^i, \omega_z^i$ from

$$\omega_x^i \bar{\Psi}_{xn} + \omega_y^i \bar{\Psi}_{yn} + \omega_z^i \bar{\Psi}_{zn} = C^{-\frac{1}{2}} \bar{D}_n^i - \left(C^{-\frac{1}{2}} (\{T_x\} \bar{\Phi}^T + \{T_y\} \bar{\Phi}_y^T + \{T_z\} \bar{\Phi}_z^T) \right)_n^i, \text{ wherein } C \text{ is a}$$

constant $(N_1-1) \times (N_1-1)$ matrix with $C_{ii'} \equiv \delta_{ii'} + 1$ and T represents the translation.

8. (Currently Amended) A method for recovering 3D An image processing method for recovery of a scene structure and camera motion from successive image data obtained from a multi-image sequence, wherein a reference image of the sequence is taken by a camera at a reference perspective and one or more successive images of the sequence are taken at one or more successive different perspectives by translating and/or rotating the camera, the method comprising the steps of:

- (a) initially recovering and compensating for camera rotation after warping the comparing a reference image to successive images, wherein the successive image is taken by translating or rotating the camera by the previously estimated translational displacements;
- (b) determining image data shifts for each successive image with respect to the reference image; the shifts being derived from the camera translation and/or rotation from the reference perspective to the successive different perspectives compensating for camera rotation after warping the reference image by an estimated translation value;
- (c) constructing a shift data matrix that incorporates determining the image data shifts for the successive images with respect to reference each image;
- (d) modifying the image shifts by multiplying the image shifts δA_i^i , s_m^i , ΔI_n^i and redefining these quantities to include the denominator factors $1 - Q_z^{-1}T_z$ for points, $1 - Z^{-1}T_z$ for intensities and $1 - B \cdot T$ for lines where $s_m^i = q_m^i - q_m^0$ and denotes the image displacement for the m -th tracked point, where ΔI_n^i is the change in image intensity and where T^i denotes the i -th intensity image and where $I_n^i = I^i(p_n)$ denotes the image intensity at the n -th pixel position in T^i and where δA_i^i represents the line flow constructing a shift data representation from each image data shift;

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(e) calculating two rank-3 factor matrices from the modified shift data matrix using SVD, one rank-3 factor matrix corresponding to the 3D structure and the other rank-3 factor matrix corresponding to the camera motion; modifying the image shift representation by multiplying the image shifts by a predetermined factor which is dependent upon the image data, said image data being one or more characteristics selected from a group consisting of points, lines and intensities;

(f) recovering calculating a first representation and a second representation from the modified shift data representation, said first representation corresponding to the 3D structure and said second representation corresponding to the camera motion; from the 3D structure matrix by solving a linear equation; and

(g) recovering reconstructing the direction of the camera motion and 3D structure from the first and second representations. camera motion matrix using the recovered 3D structure.

9. (Original) The method of claim 8, wherein the image data is one or more selected from the group consisting of points, lines and intensities.

10. (Original) The method of claim 8, wherein step (b) comprises:

computing H and \bar{D}_{CH} , where H is a $(N_{tot} - 3) \times N_{tot}$ matrix and $\bar{D}_{CH} \equiv C^{-1/2} \bar{D} H^T$ and $N_{tot} \equiv 2N_p + 2N_L + N_X$, where N_p , N_L , and N_X equals the number of points, lines and intensities, respectively, and C is a $(N_l - 1) \times (N_l - 1)$ matrix with $C_{ii'} \equiv \delta_{ii'} + 1$ where $C_{ii'}$ is a constant table of values for all images and $\delta_{ii'}$ is an operator equal to 1 if $i = i'$ and 0 if $i \neq i'$ and $\bar{D} \equiv [S \omega_L \Lambda \omega_L \Delta]$, H^T is the transpose of the H matrix, where H is a matrix defined such

that H^T is an identity matrix and annihilates $\bar{\Psi}_x, \bar{\Psi}_y, \bar{\Psi}_z$ where $\bar{\Psi}_x^T \equiv [\Psi_x^T \omega_L \Psi_{Lx}^T \omega_L \Psi_x^T]$ and similarly for the y and z components and where ω_L and ω_U are constant weights that the user sets, and where $\Psi_{Lx} \equiv \begin{bmatrix} \{P_U \cdot (\hat{x} \times A)\} \\ \{P_L \cdot (\hat{x} \times A)\} \end{bmatrix}, \Psi_{Ly} \equiv \begin{bmatrix} \{P_U \cdot (\hat{y} \times A)\} \\ \{P_L \cdot (\hat{y} \times A)\} \end{bmatrix}, \Psi_{Lz} \equiv \begin{bmatrix} \{P_U \cdot (\hat{z} \times A)\} \\ \{P_L \cdot (\hat{z} \times A)\} \end{bmatrix}$ where A is the unit normal to the plane containing the line L and the camera center at the reference image, and where $\hat{x}, \hat{y}, \hat{z}$ are unit vectors in the x, y and z directions, and where

$$\Psi_x \equiv \begin{bmatrix} \{r_x^{(1)}(q)\} \\ \{r_y^{(1)}(q)\} \end{bmatrix}, \Psi_y \equiv \begin{bmatrix} \{r_x^{(2)}(q)\} \\ \{r_y^{(2)}(q)\} \end{bmatrix}, \Psi_z \equiv \begin{bmatrix} \{r_x^{(3)}(q)\} \\ \{r_y^{(3)}(q)\} \end{bmatrix} \text{ where } q = (x, y) \text{ is the image position of the tracked point in the reference image and}$$

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the three point rotational flows $r^{(1)}(x, y), r^{(2)}(x, y), r^{(3)}(x, y)$ are defined by

$$[r^{(1)}, r^{(1)}, r^{(1)}] \equiv \left[\begin{pmatrix} -xy \\ -(1+y^2) \end{pmatrix}, \begin{pmatrix} 1+x^2 \\ xy \end{pmatrix}, \begin{pmatrix} -y \\ x \end{pmatrix} \right] \text{ and where}$$

$\Psi_{lx} \equiv -\{\nabla I \cdot r^{(1)}(p)\}, \Psi_{ly} \equiv -\{\nabla I \cdot r^{(2)}(p)\}, \Psi_{lz} \equiv -\{\nabla I \cdot r^{(3)}(p)\}$, and where p gives the image coordinates of the pixel positions, and

where Λ is an $N_i \times 2N_L$ matrix where each row corresponds to a different image i and equals $\left[\{P_U \cdot \delta A^i\}^T \{P_L \cdot \delta A^i\}^T \right]$ where P_U and P_L are a unit 3-vector projecting onto two directions $A_i \times (\hat{z} \times A_i)$ and $\hat{z} \times A_i$ which we refer to respectively as the upper and lower directions, where δA^i is the line flow $\delta A_i^i \equiv A_i^i - A_i^0$, and \hat{z} is the unit vector in the z direction and where S is a $N_i \times 2N_p$ matrix where each row corresponds to a different image i and equals $\left[\{s_x^i\}^T \{s_y^i\}^T \right]$, where $s_m^i \equiv q_m^i - q_m^0$ and denotes the image displacement for the m -th tracked

point and where Δ is a $N_I \times N_x$ matrix, where each row corresponds to an image i and equals $\{\Delta I^i\}^T$ where ΔI is the change in image intensity with respect to the reference image and where I^i denotes the i -th intensity image and where $I_n^i = I^i(p_n)$ denotes the image intensity at the n -th pixel position in I^i and where the notation $\{V\}$ is used to denote a vector with elements given by the V^a .

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11. (Currently Amended) The method of claim 8, wherein step (d) comprises:

A3 computing the a-best rank-3 factorization of $\bar{D}_{CH} \approx M^{(3)}S^{(3)T}$ where $M^{(3)}, S^{(3)}$ are rank 3 matrices corresponding respectively to motion and structure, using SVD.

12. (Original) The method of claim 8, wherein step (e) comprises:

eliminating structure unknowns Q_z , B_z and Z^{-1} from the $\bar{\Phi}_a$ to get $3N_{tot}$ linear constraints on the U and Ω using the linear equation, $[\bar{\Phi}_x \bar{\Phi}_y \bar{\Phi}_z] = H^T S^{(3)} U + [\bar{\Psi}_x \bar{\Psi}_y \bar{\Psi}_z] \Omega$, where U and Ω are unknown 3×3 matrices, and $\bar{\Phi}$ and $\bar{\Psi}$ represent total translational and rotational flow vectors respectively, and solving these constraints with $O(N_{tot})$ computations using the

SVD, where the total translational flow vectors are defined by $\bar{\Phi}_x \equiv \begin{bmatrix} \Phi_x \\ \omega_L \Phi_{Lx} \\ \omega_I \Phi_{Ix} \end{bmatrix}$ and similarly

for the y and z components, and

$\Phi_{Lx} \equiv \begin{bmatrix} \{A_x B_U\} \\ \{A_x B_L\} \end{bmatrix}$, $\Phi_{Ly} \equiv \begin{bmatrix} \{A_y B_U\} \\ \{A_y B_L\} \end{bmatrix}$, $\Phi_{Lz} \equiv \begin{bmatrix} \{A_z B_U\} \\ \{A_z B_L\} \end{bmatrix}$ where A is the normal to a first plane that passes through the center of projection and the imaged line in the reference image, and the normal to a second plane, B is defined by requiring $B \cdot A = 0$ and $B \cdot Q = -1$ for any point Q on the 3D line L,

and where $B_U \equiv B \cdot P_U$ and $B_L \equiv B \cdot P_L$ are the upper and lower components of B, and where

$$\Phi_x \equiv -\begin{bmatrix} \{Q_z^{-1}\} \\ \{0\} \end{bmatrix}, \Phi_y \equiv -\begin{bmatrix} \{0\} \\ \{Q_z^{-1}\} \end{bmatrix}, \Phi_z \equiv -\begin{bmatrix} \{q_x Q_z^{-1}\} \\ \{q_y Q_z^{-1}\} \end{bmatrix}$$

and where

$$\Phi_{Ix} \equiv -\{Z^{-1} I_x\}, \Phi_{Iy} \equiv -\{Z^{-1} I_y\}, \Phi_{Iz} \equiv \{Z^{-1} (\nabla I \cdot p)\}, \text{ and}$$

where Q is the 3d coordinate for a tracked 3D point in the reference image, and Z_n is the depth from the camera to the 3D point imaged at the n -th pixel along the cameras optical axis; and

recovering the structure unknowns Q_z , B_z and Z^{-1} from

$$[\bar{\Phi}_x \bar{\Phi}_y \bar{\Phi}_z] = H^T S^{(3)} U + [\bar{\Psi}_x \bar{\Psi}_y \bar{\Psi}_z] \Omega, \text{ given } U \text{ and } \Omega.$$

13. (Original) The method of claim 8, wherein step (f) comprises:

using $S^{(3)} U \approx [\bar{\Phi}_x \bar{\Phi}_y \bar{\Phi}_z]$ and

$\bar{D}_{CH} \approx C^{-\frac{1}{2}} \{T_x\} \bar{\Phi}^T H^T + C^{-\frac{1}{2}} \{T_y\} \bar{\Phi}_y^T H^T + C^{-\frac{1}{2}} \{T_z\} \bar{\Phi}_z^T H^T$ to recover the translations, and

recovering the rotations $\omega_x^i, \omega_y^i, \omega_z^i$ from

$$\omega_x^i \bar{\Psi}_{xn} + \omega_y^i \bar{\Psi}_{yn} + \omega_z^i \bar{\Psi}_{zn} = C^{-\frac{1}{2}} \bar{D}_n^i - \left(C^{-\frac{1}{2}} (\{T_x\} \bar{\Phi}^T + \{T_y\} \bar{\Phi}_y^T + \{T_z\} \bar{\Phi}_z^T) \right)_n^i, \text{ wherein } C \text{ is a}$$

constant $(N_1-1) \times (N_1-1)$ matrix with $C_{ii} \equiv \delta_{ii} + 1$ and T represents the translation.

14. (New) A computer system for recovering scene structure and camera motion direction from successive image data obtained from a multi-image sequence comprising:

- a processor;
- a video source whose output is digitized into a pixel map by a digitizer, said output is sent in electronic form via a system bus for access by main memory;
- a display means;
- a user interaction means for selecting items on the display means;
- a storage device in communication with said processor, said storage device stores program code for programming said processor to perform a method comprising the steps of:
- (a) comparing a reference image to successive images, wherein the successive image is taken by translating or rotating the camera;
 - (b) compensating for camera rotation after warping the reference image by a estimated translation value;
 - (c) determining the image data shift for the successive images with respect to the reference image;
 - (d) constructing a shift data representation from the image data shift;

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- (e) modifying the image shift representation by multiplying the image shifts by a predetermined factor which is dependant upon the image data, said image data being one or more characteristics selected from a group consisting of points, lines and intensities;
- (f) calculating a first representation and a second representation from the modified shift data representation, said first representation corresponding to the 3D structure and said second representation corresponding to the camera motion;
- (g) reconstructing the direction of the camera motion and 3D structure from the first and second representations.

15. (New) A computer-readable medium that includes instructions for recovering 3D scene structure and camera motion direction from image data obtained from a multi-image sequence wherein said instructions, when executed by a processor, cause the processor to:

- (a) compare a reference image to successive images, wherein the successive image is taken by translating or rotating the camera;
- (b) compensate for camera rotation after warping the reference image by a estimated translation value;
- (c) determine the image data shift for each successive image with respect to the reference image;
- (d) construct a shift data representation from the image data shift;
- (e) modifying the image shift representation by multiplying the image shifts by a predetermined factor which is dependant upon the image data, said image data being one or more characteristics selected from a group consisting of points, lines and intensities;

- (f) calculating a first representation and a second representation from the modified shift data representation, said first representation corresponding to the 3D structure and said second representation corresponding to the camera motion;
- (g) reconstructing the direction of the camera motion and 3D structure from the first and second representations.

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16. (New) The method of Claim 1, wherein shift data representations comprise a first matrix corresponding to the 3D structure and a second matrix corresponding to the camera motion.
